Chapter 17 – Additional Aspects of Aqueous Equilibria

• 17.1 The Common Ion Effect

- common ions: when two different solutes give rise to the same ion (cation/anion)
 - -- e.g. NaCl and HCl both give rise to Cl
 - -- by having two sources of the same ion we will repress the dissociation of the acid or base under examination
- common ion effect: a shift in equilibrium due to the addition of a common ion
 - -- based on Le Châtelier's Principle
 - -- example: $H_2CO_{3(aq)} + H_2O_{(l)} \rightleftharpoons HCO_{3(aq)}^- + H_3O_{(aq)}^+$
 - --- if we add $HCO_{3(aq)}^-$ then the eq shifts to the left
 - --- therefore we will not produce as much $\,H_{\scriptstyle 3}O^{\scriptscriptstyle +}_{\scriptscriptstyle (aq)}$
 - --- we will have a higher pH than we would have had
 - -- example: Calculate the pH of a solution prepared by mixing equal volumes of 0.20 $\underline{\text{M}}$ CH₃NH₂ and 0.60 $\underline{\text{M}}$ CH₃NH₃Cl (K_b = 3.7 x 10⁻⁴). What is the pH of 0.20 $\underline{\text{M}}$ CH₃NH₂ without addition of CH₃NH₃Cl? assuming we have 1 L of each

$$\left[CH_3NH_2 \right]_0 = \frac{0.20 \, moles \, CH_3NH_2}{L} \times 1L \\ = 0.10 \, \underline{M} \, CH_3NH_2$$

$$\left[CH_{3}NH_{3}^{+}\right]_{0} = \frac{\underbrace{0.60\,moles\,CH_{3}NH_{3}^{+}}_{L}\times1L}{2.0\,L} = 0.30\,\underline{M}\,CH_{3}NH_{3}^{+}$$

I	0.1	-	0.3	0
С	-X	-	+x	+x
E	0.1 - x	-	0.3 + x	+x

$$K_b = \frac{[CH_3NH_3^+][OH^-]}{[CH_3NH_2]} = \frac{(0.3+x)x}{0.1-x} = 3.7 \times 10^{-4}$$

$$x^2 + 0.3004x - 3.7 \times 10^{-5} = 0$$

$$x = 8.97 \times 10^{-5} \, \underline{M} \, OH^{-}$$

$$pH = 14 + \log(8.97 \times 10^{-5}) = 9.95$$

pH of 0.20 M CH₃NH₂:

$$K_b = \frac{[CH_3NH_3^+][OH^-]}{[CH_3NH_2]} = \frac{x^2}{0.1 - x} = 3.7 \times 10^{-4}$$

$$x^2 + 3.7 \times 10^{-4} x - 3.7 \times 10^{-5} = 0$$

$$x = 8.24 \times 10^{-3} \underline{M} OH^-$$

$$pH = 14 + \log(8.24 \times 10^{-3}) = 11.92$$

• 17.2 Buffers

- pH buffer: a solution that resists changes in pH
 - -- they are made with solutions which have either a base and its conj acid or with an acid and its conj base

- -- therefore the result of the common-ion effect
- buffer capacity: the quantity of acid/base needed to significantly change the pH of a buffer
 - -- the larger the buffer capacity the larger this amount is
 - -- depends upon the number of moles of acid/base are present in solution
 - --- for equal volumes the more concentrated the solutions the larger the buffer capacity
 - --- for equal moles of acid/base the larger the volume the larger the buffer capacity
- Henderson-Hasselbalch MEMORIZE!
 - -- we use this equation when we need to make or have a buffer
 - -- Ex: Calculate the pH and pOH of a 500.0mL solution containing

0.225M HPO_4^{2-} and 0.225M PO_4^{3-} at 25°C where the $K_a(HPO_4^{2-}) = 4.2 \times 10^{-13}$.

$$pH = pK_a + \log\left(\frac{[A^-]}{[HA]}\right) = -\log(4.2 \times 10^{-13}) + \log\left(\frac{0.225M}{0.225M}\right)$$
$$pH = 12.38$$

-- Ex: How would we prepare a pH = 4.44 buffer using CH₃CO₂H and CH₃CO₂Na? $K_a = 1.8 \times 10^{-5}$

$$pH = pK_a + \log\left(\frac{[A^-]}{[HA]}\right) \to \log\left(\frac{[CH_3CO_2^-]}{[CH_3CO_2H]}\right) = 4.44 + \log(1.8 \times 10^{-5}) = -0.305$$

$$\frac{[CH_3CO_2^-]}{[CH_3CO_2H]} = 10^{-0.305} = 0.496$$

Therefore, in order to make a 4.44 buffer solution we need 0.496 moles of CH_3CO_2Na for every mole of CH_3CO_2H

-- Here are a set of examples which show how pH is impacted starting with a weak acid, then looking at a salt solution with the weak acid's conjugate base, then we put the two together forming a buffer and finally we see the effect of adding a small amount of acid and base to a buffer

a. 0.100 M
$$HC_3H_5O_2$$
, $K_a=1.3\times10^{-5}$

$$HC_3H_5O_2 \rightleftharpoons H^+ + C_3H_5O_2^- \rightarrow K_a = \frac{\left[H^+\right]\left[C_3H_5O_2^-\right]}{\left[HC_3H_5O_2\right]}$$

$$1.3 \times 10^{-5} = \frac{x^2}{0.100 - x} \to x = 1.1 \times 10^{-3} M \ H^+ \quad pH = 2.96$$

b. 0.100 M $NaC_{2}H_{5}O_{7}$

$$NaC_{3}H_{5}O_{2} \rightarrow Na^{+} + C_{3}H_{5}O_{2}^{-}$$

$$C_{3}H_{5}O_{2}^{-} + H_{2}O \rightleftharpoons OH^{-} + HC_{3}H_{5}O_{2} \rightarrow K_{b} = \frac{K_{w}}{K_{a}} = \frac{\left[OH^{-}\right]\left[HC_{3}H_{5}O_{2}\right]}{\left\lceil C_{3}H_{5}O_{2}^{-}\right\rceil}$$

$$7.7 \times 10^{-10} = \frac{x^2}{0.100 - x} \approx \frac{x^2}{0.100} \rightarrow x = 8.8 \times 10^{-6} M \ OH^- \quad pH = 14 - pOH = 8.94$$

c. a mixture containing a. & b.

$$HC_3H_5O_2 \rightleftharpoons H^+ + C_3H_5O_2^- \rightarrow K_a = \frac{\left\lfloor H^+ \right\rfloor \left\lfloor C_3H_5O_2^- \right\rfloor}{\left\lfloor HC_3H_5O_2 \right\rfloor}$$

$$1.3 \times 10^{-5} = \frac{(0.100 + x)x}{0.100 - x} \rightarrow x = 1.3 \times 10^{-5} M \ H^{+} \quad pH = 4.89$$

using Henderson-Hasselbach,
$$pH = pKa + \log \left(\begin{bmatrix} A^- \end{bmatrix} \right)$$
 [HA]

$$pH = -\log 1.3 \times 10^{-5} + \log \left(\frac{0.100}{0.100} \right) = 4.89$$

d. a mixture containing c. and 0.020 mol of NaOH

when strong base is added to an acid containing solution it will neutralize the acid and so all of the OH⁻ will react completely with our propanoic acid

$$HC_3H_5O_2 + OH^- \rightleftharpoons H_2O + C_3H_5O_2^-$$

	$HC_3H_5O_2$	OH^-	$C_3H_5O_2^-$
В	0.100	0.020	0.100
С	-0.020	-0.020	+0.02
Α	0.080	0	0.120

$$pH = -\log 1.3 \times 10^{-5} + \log \left(\frac{0.120}{0.080} \right) = 5.06$$

e. a mixture containing c. and 0.020 mol of HCl

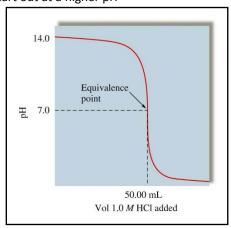
$$H^+ + C_3H_5O_2^- \rightleftharpoons HC_3H_5O_2$$

	* * - * -					
	$C_{3}H_{5}O_{2}^{-}$	$H^{^+}$	$HC_3H_5O_2$			
В	0.100	0.020	0.100			
С	-0.020	-0.020	+0.02			
A	0.080	0	0.120			

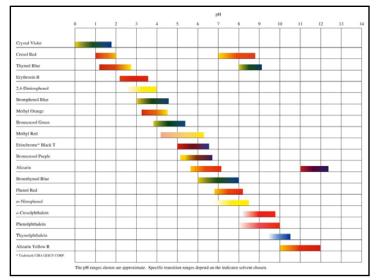
$$pH = -\log 1.3 \times 10^{-5} + \log \left(\frac{0.080}{0.120} \right) = 4.71$$

• 17.3 Acid-Base Titrations

- we do titrations to determine conc'ns of species
- we continue to add titrant until we have exactly the correct number of moles of titrant to neutralize that of the analyte we are measuring
 - -- when this occurs we have reached the endpoint or equivalence point
- pH versus volume the titration curve
 - -- when a single endpt occurs there is only one species interacting with the titrant e.g. HCl + NaOH
 - -- when more than one species is reacting with the titrant we will have two endpts e.g. K⁺ + Fe³⁺ + NaOH
 - -- if acid is the titrant, we start out at a higher pH

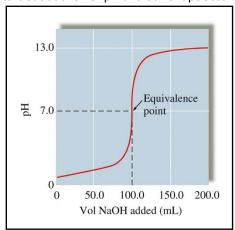


- --- if we use a strong acid with a strong base, our endpt occurs at pH = 7
 - ---- for this situation we want an indicator that has a color change of around pH 7 which according to our indicator chart see



--- if we use a strong acid with a weak base, our endpt occurs at pH < 7
---- indicators, range from crystal violet to bromothymol blue

-- if base is the titrant, we start out at a lower pH and our endpt occurs at a higher pH



--- if we use a strong base with a weak acid, our endpt occurs at a pH > 7

---- indicators, range from phenol red to alizarin yellow R and possibly thymol blue

- Ex: What is [NH₃] if 22.35mL of 0.1145 M HCl were needed to titrate a 100.0mL sample?

$$NH_3 + HCl \rightleftharpoons NH_4^+ + Cl^-$$

$$[NH_3] = 0.02235L \times \frac{0.1145 \ moles \ HCl}{L} \times \frac{1 \ mole \ NH_3}{1 \ mole \ HCl} \times \frac{1}{0.1000L} = 0.02259 \underline{M}$$

- Titration Examples:
 - -- The Strong & The Weak:

A 25.0 mL sample of 0.100 M acetic acid ($HC_2H_3O_2$) is titrated with 0.125 M of NaOH. Calculate the pH of the mixture after 10.0, 20.0, and 30.0 mL of base have been added. ($K_a = 1.8 \times 10^{-5}$)

Initially we have:

$$HC_2H_3O_{2(aq)} + NaOH_{(aq)} \rightarrow NaC_2H_3O_{2(aq)} + H_2O_{(l)}$$

 Na^+ is a spectator ion so we are really looking at:

$$HC_2H_3O_{2(aq)} + OH_{(aq)}^- \to C_2H_3O_{2(aq)}^- + H_2O_{(l)}$$

This is in fact a neutralization reaction. For 10.0 mL of NaOH:

$$25.0 \; mL \times \frac{1 \; L}{1000 \; mL} \times \frac{0.100 \; mol \; HC_2H_3O_{2(aq)}}{1 \; L} = 0.00250 \; mol \; HC_2H_3O_{2(aq)}$$

$$10.0 \ mL \times \frac{1 \ L}{1000 \ mL} \times \frac{0.125 \ mol \ OH^{-}_{(aq)}}{1 \ L} = 0.00125 \ mol \ OH^{-}_{(aq)}$$

Now we set up a "BCA" table or before, change, after table (it is in mol not mol/L hence the difference)

So, we have neutralized the acid with the given amount of base and are now ready to apply the Henderson-Hasselbalch equation:

$$pH = pK_a + \log\left(\frac{A^-}{[HA]}\right) = -\log\left(1.8 \times 10^{-5}\right) + \log\left(\frac{0.0125}{0.0350L}\right) = 4.74$$

Time for 20.0 mL of NaOH:

$$20.0 \ mL \times \frac{1 \ L}{1000 \ mL} \times \frac{0.125 \ mol \ OH_{(aq)}^{-}}{1 \ L} = 0.00250 \ mol \ OH_{(aq)}^{-}$$

$$HC_{2}H_{3}O_{2(aq)} \ + \ OH_{(aq)}^{-} \rightarrow \ C_{2}H_{3}O_{2(aq)}^{-} \ + \ H_{2}O_{(l)}$$

$$B \qquad 0.00250 \qquad 0.00250 \qquad 0 \qquad -$$

$$C \qquad -0.00250 \qquad -0.00250 \qquad +0.00250 \qquad -$$

$$A \qquad 0 \qquad 0 \qquad +0.00250 \qquad -$$

All of the acid has reacted with all the base and so we are now at the equivalence point. However, since we had a weak acid and a strong base we should expect our pH to be higher than 7. To find the pH we need an "ICE" table.

$$\begin{bmatrix} C_2 H_3 O_{2(aq)}^- \end{bmatrix} = 0.00250 \; moles \; / \; 0.045 L = 0.0556 \underline{M}$$

$$C_2 H_3 O_{2(aq)}^- \; + \; H_2 O_{(l)} \to \; H C_2 H_3 O_{2(aq)} \; + \; O H_{(aq)}^-$$

$$\begin{matrix} \text{I} & 0.0556 & - & 0 & 0 \\ \text{C} & -\text{x} & - & +\text{x} & +\text{x} \\ \text{E} & 0.0556 -\text{x} & - & +\text{x} & +\text{x} \end{matrix}$$

$$\begin{split} K_b &= \frac{\left[HC_2H_3O_{2(aq)}\right]\left[OH_{(aq)}^-\right]}{\left[C_2H_3O_{2(aq)}^-\right]} = \frac{K_w}{K_a} = \frac{10^{-14}}{1.8\times10^{-5}} = 5.6\times10^{-10} = \frac{x^2}{0.0556-x} \\ assume \ x \ll 0.0556 \quad 5.6\times10^{-10} \sim \frac{x^2}{0.0556} \quad x = \left[OH_{(aq)}^-\right] = 5.6\times10^{-6}M \\ ck \ assumption: \quad \frac{5.6\times10^{-6}}{0.0556}\times100\% = 0.01\% < 5\% \\ pH &= 14 + \log(5.6\times10^{-6}) = 8.75 \end{split}$$

Finally, 30.0 mL

$$30.0 \ mL \times \frac{1 \ L}{1000 \ mL} \times \frac{0.125 \ mol \ OH_{(aq)}^{-}}{1 \ L} = 0.00375 \ mol \ OH_{(aq)}^{-}$$

Now, we have more strong base than acid so we can set up the BCA table and then determine hydroxide concentration and pH directly.

$$\begin{split} HC_2H_3O_{2(aq)} &+ OH^-_{(aq)} \rightarrow C_2H_3O^-_{2(aq)} &+ H_2O_{(l)} \\ \text{B} & 0.00250 & 0.00375 & 0 & - \\ \text{C} & -0.00250 & -0.00250 & - \\ \text{A} & 0 & 0.00125 & +0.00375 & - \\ & & OH^- \end{bmatrix} = \frac{0.00125 \ moles}{0.055L} = 0.0227M \\ pH &= 14 + \log(0.0227) = 12.36 \end{split}$$

- The Strong & the Strong: HCl & NaOH

A 15.0 mL sample of 0.200 M NaOH is titrated with 0. 250 M of HCl. Calculate the pH of the mixture after 10.0, and 20.0 mL of acid have been added.

If you are not given a dissociation constant this should remind you that the acid/base is strong. For 10.0 mL of HCl & 15.0 mL of NaOH:

$$\begin{split} 10.0 \ mL \times \frac{1 \ L}{1000 \ mL} \times \frac{0.250 \ mol \ H_{(aq)}^{^{+}}}{1 \ L} &= 0.00250 \ mol \ H_{(aq)}^{^{+}} \\ 15.0 \ mL \times \frac{1 \ L}{1000 \ mL} \times \frac{0.200 \ mol \ OH_{(aq)}^{^{-}}}{1 \ L} &= 0.00300 \ mol \ OH_{(aq)}^{^{-}} \\ &\qquad \qquad H_{(aq)}^{^{+}} + OH_{(aq)}^{^{-}} \rightarrow H_2O_{(l)} \\ &\qquad \qquad B \qquad 0.00250 \qquad 0.00300 \qquad - \\ &\qquad \qquad C \qquad -0.00250 \qquad -0.00250 \qquad - \\ &\qquad \qquad A \qquad 0 \qquad 0.00050 \qquad - \\ &\qquad \left[OH^{-}\right] = \frac{0.0005 \ moles}{0.025L} = 0.0200M \\ pH = 14 + \log(0.02) = 12.30 \end{split}$$

For 20.0 mL of HCl

$$20.0 \ mL \times \frac{1 \ L}{1000 \ mL} \times \frac{0.250 \ mol \ H_{(aq)}^+}{1 \ L} = 0.00500 \ mol \ H_{(aq)}^+$$

$$H_{(aq)}^+ + OH_{(aq)}^- \rightarrow H_2O_{(l)}$$

$$B \quad 0.00500 \quad 0.00300 \quad -$$

$$C \quad -0.00300 \quad -0.00300 \quad -$$

$$A \quad 0.00200 \quad 0 \quad -$$

$$[H^+] = \frac{0.002 \text{ moles}}{0.035L} = 0.05714M$$
$$pH = -\log(0.05714) = 1.24$$

- Titrations of Polyprotic Acids - SKIP!

• 17.4 Solubility Equilibria

- K_{sp} is called the solubility product and is the eq constant for solids in solution

$$CaF_{2(s)} \rightleftharpoons Ca_{(aq)}^{2+} + 2F_{(aq)}^{-}$$
 $K_{sp} = 3.9 \times 10^{-11}$
 $K_{sp} = [Ca_{(aq)}^{2+}][F_{(aq)}^{-}]^{2}$

- In general, $M_m X_x \rightleftharpoons m M_{(aq)} + x X_{(aq)} \qquad K_{sp} = [M]^m [X]^x$
- Ex: Determine the equilibrium concentrations (and solubilities) of $BaF_{2(s)}$, $K_{sp} = 1.7x10^{-6}$.

$$BaF_{2(s)} \rightleftharpoons Ba_{(aq)}^{2+} + 2F_{(aq)}^{-} \qquad 1.7 \times 10^{-6}$$

$$s \qquad 2s$$

$$K_{sp} = [S][2S]^{2}$$

$$1.7 \times 10^{-6} = 4S^{3} \rightarrow S = 0.0075\underline{M}$$

$$[Ba^{2+}] = 0.0075\underline{M} \quad and \quad [F^{-}] = 2 \times 0.0075 = 0.015\underline{M}$$

$$Ba^{2+} : \frac{0.0075 \, moles}{L} \times \frac{137.327 \, g}{mol} = 1.03 \frac{g}{L}$$

$$F^{-} : \frac{0.015 \, moles}{L} \times \frac{18.998 \, g}{mol} = 0.285 \frac{g}{L}$$

• 17.5 Factors that Affect Solubility

- common ion effect -- just like it affects the pH it will affect our solubility
- -- to deal with this problem we must once again invoke the ICE table
 - -- Ex: Calculate the solubility of calcite (CaCO₃) in 0.00100 M of Na_2CO_3 ($K_{sp} = 4.5 \times 10^{-9}$ at 25° C).

$$\begin{array}{c|c} CaCO_{3(s)} \rightleftharpoons Ca_{(aq)}^{2+} + CO_{(aq)}^{2-} \\ \hline & Ca_{(aq)}^{2+} & CO_{(aq)}^{2-} \\ \hline \text{Initial} & 0 & 0.0010 \\ \hline \text{Change} & +s & +s \\ \hline \text{Eq} & s & 0.0010+s \\ \hline \end{array}$$

$$K_{sp} = [s][0.001 + s]$$

assume $0.001 >> s$
 $K_{sp} = 4.5 \times 10^{-9} \sim 0.001s \rightarrow s = 4.5 \times 10^{-6} M$
 $ck: \frac{4.5 \times 10^{-6}}{0.001} \times 100\% = 0.45\% < 5\%$

Therefore the solubility of CaCO₃ is 4.5x10⁻⁶M

- pH of solution
 - -- if a salt contains the conjugate base of a weak acid then it will be affected by the pH
 - -- ex: CaCO₃ in acidic solution

$$CaCO_{3(s)} \rightleftharpoons Ca_{(aq)}^{2+} + CO_{3(aq)}^{2-}$$

 $\underbrace{H_{(aq)}^{+} + CO_{3(aq)}^{2-}}_{CaCO_{3(s)} + H_{(aq)}^{+}} \rightleftharpoons Ca_{(aq)}^{2+} + HCO_{3(aq)}^{-}$

- --- when CaCO₃ comes into contact with acidic solution it will dissolve
- -- This will not be a factor for the conjugate bases of strong acids since they will not reform their acidic counterparts
- formation of complex ions
 - -- if a ligand is added to a solution containing the salt it could lead to complex ion formation
 - -- if this occurs then the amount of metallic cation is reduced therefore pushing eq to the right, causing the salt to become more soluble
 - -- ex: AgCl and NH₃

$$AgCl_{(s)} \rightleftharpoons Ag^{+}_{(aq)} + Cl^{-}_{(aq)}$$

$$Ag^{+}_{(aq)} + 2NH_{3(aq)} \rightleftharpoons Ag(NH_{3})^{+}_{2(aq)}$$

$$AgCl_{(s)} + 2NH_{3(aq)} \rightleftharpoons Ag(NH_{3})^{+}_{2(aq)} + Cl^{-}_{(aq)}$$

- Amphoterism SKIP!
- 17.6 Precipitation & Separation of Ions & 17.7 Qualitative Analysis for Metallic Elements Skip!